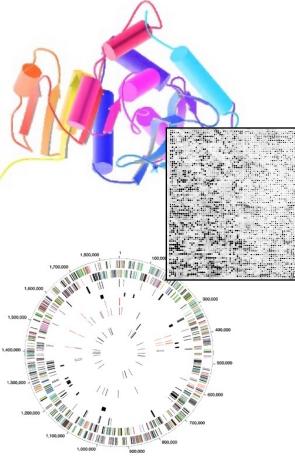
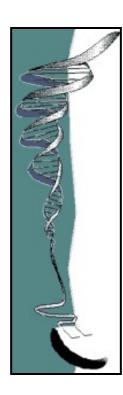
Biomedical Data Science: Analysis of Network Topology B – Network Quantities



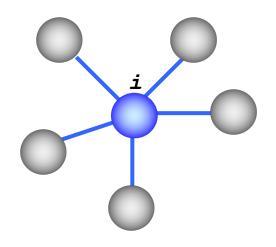


Mark Gerstein, Yale University gersteinlab.org/courses/452 (last edit in spring '21, final)



Network Topology

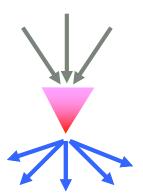
What are the Main Quantities that Can be Calculated from Networks? • Degree of a node: the number of edges incident on the node



Degree of node i = 5

Network parameters

Number of incoming and outgoing connections



Incoming connections = 2.2 \rightarrow each gene is regulated by ~ 2 TFs

In-degree

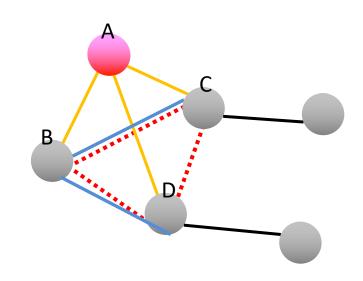
Outgoing connections = 20.2 → each TF regulates ~20 genes

Out-degree

Connectivity

Clustering coefficient

- Clustering Coefficient:
 - Ratio of existing links to maximum number of links for neighbouring nodes
 - Example:
 - For A:
 - •3 neighbours
 - •2 existing link
 - •3 possible links
 - Clustering coefficient
 - C_A=2/3



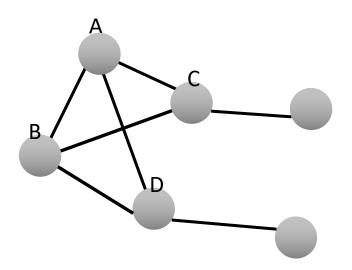
Example from: http://www.learner.org/courses/mathilluminated/units/11/textbook/04.php

Clustering coefficient

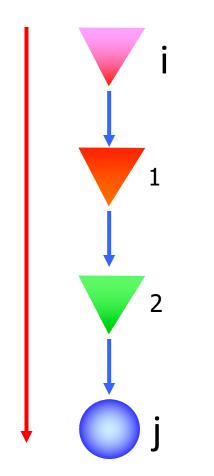
- Average Coefficient:
 - Average of clustering coefficients of all nodes n

$$\overline{C} = \frac{1}{n} \sum_{i=1}^{n} C_i$$

- Measure of inter-connectedness of the network
- Global property
- Example:
 - Clustering coefficient:
 - C_A=2/3 C_B=2/3
 - $C_{C}=1/3$ $C_{D}=1/3$
 - Average coefficient =
 - 1/4(2/3+2/3+1/3+1/3) = 0.5



Path length

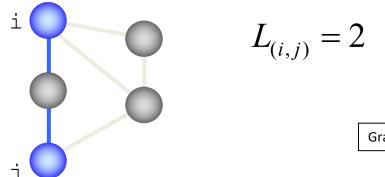


- Number of edges along a path
- Path length = 3
- Meaning:
 - Number of intermediate TFs to reach final target
 - Indication of how immediate a response is

Path length

Shortest path length:

• $L_{(i,j)}$ is the minimum number of edges that must be traversed to travel from a vertex i to another vertex j of a graph G



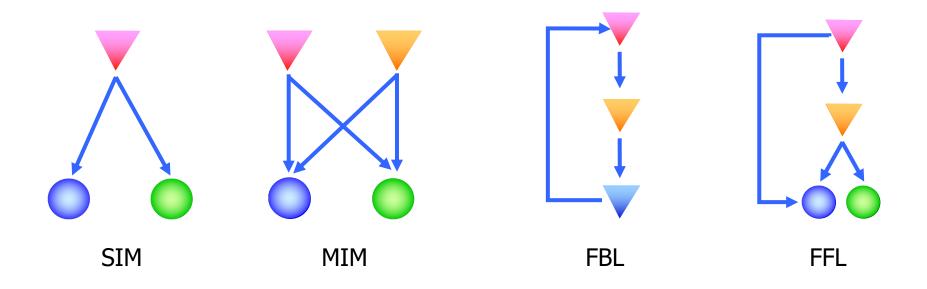
Graph Theory Terminology (Batten, pp. 92-105)

- Characteristic path length (Average path length)
 - The characteristic path length *L* of a graph is the average of the $L_{(i,j)}$ for every possible pair (i,j) $L = \frac{1}{n(n-1)} \sum_{i,j} L_{(i,j)}$
 - Networks with small values of L are said to have the "small world property"

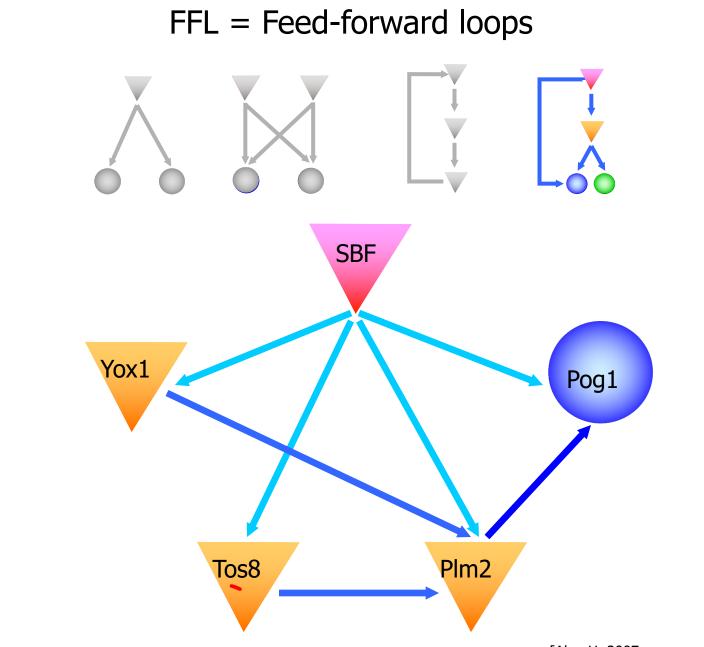
http://en.wikipedia.org/wiki/Average_path_length

Network motifs

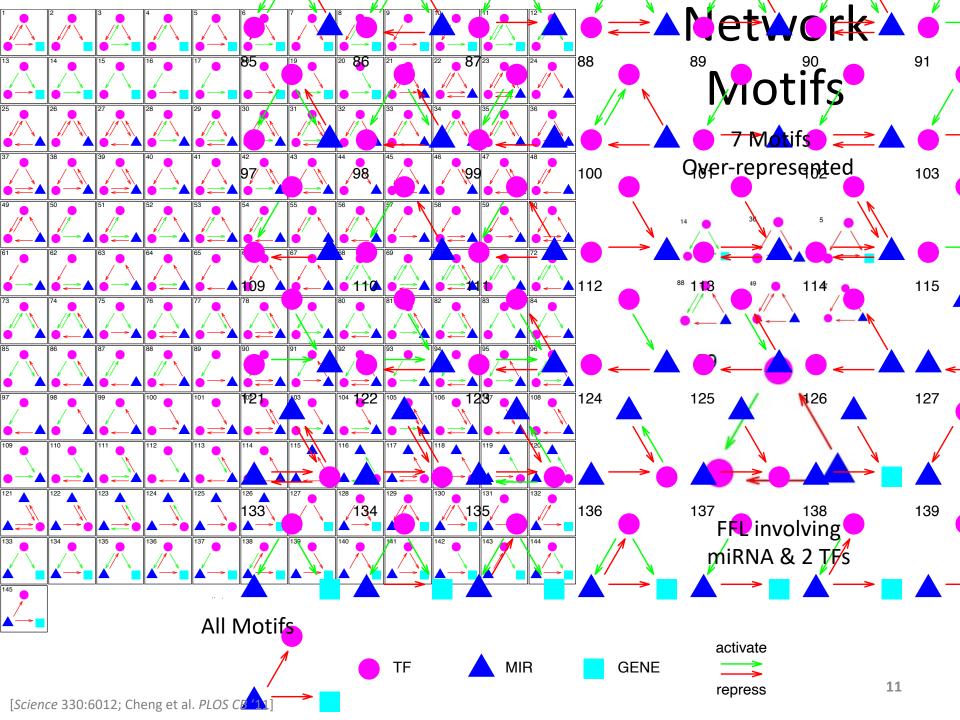
Regulatory modules within the network



[Alon U, 2007, Nature Reviews Genetics, Network motifs: theory and experimental approaches]



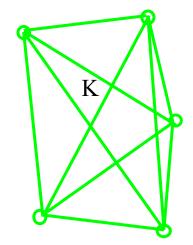
10



Cliques

- Fully connected sub-components
- Related measures
 k-cores : For all vertices in a graph G
 have degree at least k

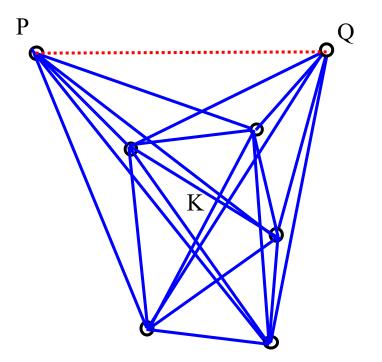
[Hogue et al, BMC BIOINFORMATICS, 2003]



Problem: High-throughput experiments are prone to missing interactions

One solution—defective cliques

- If proteins P and Q interact with a clique K of proteins which all interact with each other, then P and Q are more likely to interact with each other
- P, Q, and K form a defective clique



Predicting protein interactions by completing defective cliques